

III B.Tech.(CCC) Supplementary Examinations, June 2008
DIGITAL SIGNAL PROCESSING
(Electronics & Communication Engineering)

Time: 3 hours**Max Marks: 100**

Answer any FIVE Questions
All Questions carry equal marks

1. (a) Consider a discrete linear time invariant system described by the difference equation:

$$Y(n) - (3/4)y(n-1) + (1/8)y(n-2) = x(n) + (1/3)x(n-1)$$
 Where $y(n)$ is the output and $x(n)$ is the input.
 Assuming that the system is relaxed initially obtain the unit sample response of the system.
 (b) Find the:
 - i. impulse response
 - ii. output response for a step input applied at $n=0$ of a discrete time linear time invariant system whose difference equation is given by $y(n) = y(n-1) + 0.5 y(n-2) + x(n) + x(n-1)$. [10+10]
2. (a) An LTI system is described by the equation $y(n) = x(n) + 0.81x(n-1) - 0.81x(n-2) - 0.45y(n-2)$. Determine the transfer function of the system. Sketch the poles and zeroes on the Z-plane.
 (b) Define stable and unstable system test the condition for stability of the first-order IIR filter governed by the equation $y(n) = x(n) + bx(n-1)$. [10+10]
3. Prove the following properties of the discrete Fourier series for periodic sequences.

Sequences	Discrete Fourier Series
(a) $x(n+m)$	$W_N^{-Km} X(K)$
(b) $x^*(n)$	$X^*(-K)$
(c) $x^*(-n)$	$X^*(K)$
(d) $\text{Re}[x(n)]$	$X_e(K)$
(e) $\text{Im}[x(n)]$	$X_o(K)$ [20]
4. (a) Distinguish between DFT and DTFT .
 (b) Consider a sequence $x(n)$ of length L. Consider its DTFT $X_d(w)$ is sampled and N is the number of frequency samples. Discuss the relation between L and N for inverse DTFT = inverse DFT comment on the aliasing problem.
 (c) Compute the DFT of $x(n) = \{1, 0, 0, 0\}$ and compare with $X_d(w)$. [6+7+7]
5. (a) Implement the decimation in time FFT algorithm for N=16.
 (b) In the above Question how many non - trivial multiplications are required. [12+8]

6. Determine the system function $H(Z)$ of the lowest order Chebyshev digital filter that meets the following specifications.
- (a) 1 db ripple in the passband $0 \leq |W| \leq 0.3\pi$
 - (b) At least 60 db attenuation in the stopband $0.35\pi \leq |W| \leq \pi$. Use the bilinear transformation. [20]
7. (a) Describe the principle of designing FIR filter using DFT method.
- (b) Using frequency sampling method, design a band pass filter with the following specifications.
 Sampling frequency $F = 8000\text{Hz}$
 Cut-off frequency $f_{c1} = 1000\text{Hz}$ $f_{c2} = 3000\text{Hz}$
 Determine the filter coefficients for $N=7$. [8+12]
8. (a) Explain the different structures for realisation of IIR system. and explain how conversion can be made from direct form I structure to direct form II structure.
- (b) Realize the given system in cascade and parallel form

$$H(Z) = \frac{1 + \frac{1}{2}Z^{-1}}{\left[1 - Z^{-1} + \frac{1}{4}Z^{-2}\right]\left[1 - Z^{-1} + \frac{1}{2}Z^{-2}\right]} \quad [10+10]$$
