“Econometrics of Event Studies”

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ABSTRACT

The number of published event studies exceeds 500, and the literature continues to grow. We provide an overview of event study methods. Short-horizon methods are quite reliable. While long-horizon methods have improved, serious limitations remain. A challenge is to continue to refine long-horizon methods. We present new evidence illustrating that properties of event study methods can vary by calendar time period and can depend on event sample firm characteristics such as volatility. This reinforces the importance of using stratified samples to examine event study statistical properties.
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1. Introduction and Background

This chapter focuses on the design and statistical properties of event study methods. Event studies examine the behavior of firms’ stock prices around corporate events.\(^1\) A vast literature written over the past several decades has become an important part of financial economics. Prior to that time, “there was little evidence on the central issues of corporate finance. Now we are overwhelmed with results, mostly from event studies” (Fama, 1991, p. 1600). In a corporate context, the usefulness of event studies arises from the fact that the magnitude of abnormal performance at the time of an event provides a measure of the (unanticipated) impact of this type of event on the wealth of the firms’ claimholders. Thus, event studies focusing on announcement effects for a short-horizon around an event provide evidence relevant for understanding corporate policy decisions.

Event studies also serve an important purpose in capital market research as a way of testing market efficiency. Systematically nonzero abnormal security returns that persist after a particular type of corporate event are inconsistent with market efficiency. Accordingly, event studies focusing on long-horizons following an event can provide key evidence on market efficiency (Brown and Warner, 1980, and Fama, 1991).

Beyond financial economics, event studies are useful in related areas. For example, in the accounting literature, the effect of earnings announcements on stock prices has received

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\(^1\) We discuss event studies that focus only on the mean stock price effects. Many other types of event studies also appear in the literature, including event studies that examine return variances (e.g., Beaver, 1968, and Patell, 1976), trading volume (e.g., Beaver, 1968, and Campbell and Wasley, 1996), operating (accounting) performance (e.g., Barber and Lyon, 1996), and earnings management via discretionary accruals (e.g., Dechow, Sloan, and Sweeney, 1995, and Kothari, Leone, and Wasley, 2005).
much attention. In the field of law and economics, event studies are used to examine the effect of regulation, as well as to assess damages in legal liability cases.

The number of published event studies easily exceeds 500 (see section 2), and continues to grow. A second and parallel literature, which concentrates on the methodology of event studies, began in the 1980’s. Dozens of papers have now explicitly studied statistical properties of event study methods. Both literatures are mature.

From the methodology papers, much is known about how to do – and how not to do – an event study. While the profession’s thinking about event study methods has evolved over time, there seems to be relatively little controversy about statistical properties of event study methods. The conditions under which event studies provide information and permit reliable inferences are well-understood.

This chapter highlights key econometric issues in event study methods, and summarizes what we know about the statistical design and the interpretation of event study experiments. Based on the theoretical and empirical findings of the methodology literature, we provide clear guidelines both for producers and consumers of event studies. Rather than provide a comprehensive survey of event study methods, we seek to sift through and synthesize existing work on the subject. We provide many references and borrow heavily from the contributions of published papers. Two early papers that cover a wide range of issues are by Brown and Warner (1980, 1985). More recently, an excellent chapter in the textbook of Campbell, Lo, and MacKinlay (1997) is a careful and broad outline of key research design issues. These standard references are recommended reading, but predate important advances in our understanding of event study methods, in particular on long horizon methods. We provide an updated and much needed overview, and include a bit of new evidence as well.
Although much emphasis will be on the statistical issues, we do not view our mission as narrowly technical. As financial economists, our ultimate interest is in how to best specify and test interesting economic hypotheses using event studies. Thus, the econometric and economic issues are interrelated, and we will try to keep sight of the interrelation.

In section 2, we briefly review the event study literature and describe the changes in event study methodology over time. In Section 3 we discuss how to use events studies to test economic hypotheses. We also characterize the properties of the event study tests and how these properties depend on variables such as security volatility, sample size, horizon length, and the process generating abnormal returns. Section 4 is devoted to issues most likely encountered when conducting long-horizon event studies. The main issues are risk adjustment, cross-correlation in returns, and changes in volatility during the event period.

2. The Event Study Literature: Basic Facts

2.1 The stock and flow of event studies

To quantify the enormity of the event study literature, we conducted a census of event studies published in 5 leading journals: the Journal of Business (JB), Journal of Finance (JF), Journal of Financial Economics (JFE), Journal of Financial and Quantitative Analysis (JFQA), and the Review of Financial Studies (RFS). We began in 1974, the first year the JFE was published.

Table 1 reports the results for the years 1974 through 2000. The total number of papers reporting event study results is 565. Since many academic and practitioner-oriented journals are excluded, these figures provide a lower bound on the size of the literature. The number of papers published per year increased in the 1980’s, and the flow of papers has since been stable. The
peak years are 1983 (38 papers), 1990 (37 papers), and 2000 (37 papers). All five journals have significant representation. The JFE and JF lead, with over 200 papers each.

Table 1 makes no distinction between long horizon and short horizon studies. While the exact definition of “long horizon” is arbitrary, it generally applies to event windows of 1 year or more. Approximately 200 of the 565 event studies listed in Table 1 use a maximum window length of 12 months or more, with no obvious time trend in the year by year proportion of studies reporting a long-horizon result.


### 2.2 Changes in event study methods: the big picture

Even the most cursory perusal of event studies done over the past 30 years reveals a striking fact: the basic statistical format of event studies has not changed over time. It is still based on the table layout in the classic stock split event study of Fama, Fisher, Jensen, and Roll (1969). The key focus is still on measuring the sample securities’ mean and cumulative mean abnormal return around the time of an event.
Two main changes in methodology have taken place, however. First, the use of daily (and sometimes intraday) rather than monthly security return data has become prevalent, which permits more precise measurement of abnormal returns and more informative studies of announcement effects. Second, the methods used to estimate abnormal returns and calibrate their statistical significance have become more sophisticated. This second change is of particular importance for long-horizon event studies. The changes in long-horizon event study methods reflect new findings in the late 1990s on the statistical properties of long-horizon security returns. The change also parallels developments in the asset pricing literature, particularly the Fama-French 3-factor model.

While long-horizon methods have improved, serious limitations of long-horizon methods have been brought to light and still remain. We now know that inferences from long-horizon tests “require extreme caution” (Kothari and Warner, 1997, p. 301) and even using the best methods “the analysis of long-run abnormal returns is treacherous” (Lyon, Barber, and Tsai, 1999, p. 165). These developments underscore and dramatically strengthen earlier warnings (e.g., Brown and Warner, 1980, p. 225) about the reliability - or lack of reliability - of long-horizon methods. This contrasts with short-horizon methods, which are relatively straightforward and trouble-free. As a result, we can have more confidence and put more weight on the results of short-horizon tests than long-horizon tests. Short-horizon tests represent the “cleanest evidence we have on efficiency” (Fama, 1991, p.1602), but the interpretation of long-horizon results is problematic. As discussed later, long-horizon tests are highly susceptible to the joint-test problem, and have low power.

Of course these statements about properties of event study tests are very general. To provide a meaningful basis for assessing the usefulness of event studies - both short- and long-
horizon – it is necessary to have a framework that specifies: i) the economic and statistical hypotheses in an event study, and ii) an objective basis for measuring and comparing the performance of event study methods. Section 3 lays out this framework, and summarizes general conclusions from the methodology literature. In the remainder of the chapter, additional issues and problems are considered with more specificity.

3. Characterizing Event Study Methods

3.1 An event study: the model

An event study typically tries to examine return behavior for a sample of firms experiencing a common type of event (e.g., a stock split). The event might take place at different points in calendar time or it might be clustered at a particular date (e.g., a regulatory event affecting an industry or a subset of the population of firms). Let \( t = 0 \) represent the time of the event. For each sample security \( i \), the return on the security for time period \( t \) relative to the event, \( R_{it} \), is:

\[
R_{it} = K_{it} + e_{it}
\]

(1)

where \( K_{it} \) is the “normal” (i.e., expected or predicted return given a particular model of expected returns), and \( e_{it} \) is the component of returns which is abnormal or unexpected.\(^2\) Given this return decomposition, the abnormal return, \( e_{it} \), is the difference between the observed return and the predicted return:

\[
e_{it} = R_{it} - K_{it}
\]

(2)

Equivalently, \( e_{it} \) is the difference between the return conditional on the event and the expected return unconditional on the event. Thus, the abnormal return is a direct measure of the

\(^2\) This framework is from Brown and Warner (1980) and Campbell, Lo, and MacKinlay (1997).
A model of normal returns (i.e., expected returns unconditional on the event but conditional on other information) must be specified before an abnormal return can be defined. A variety of expected return models (e.g., market model, constant expected returns model, capital asset pricing model) have been used in event studies. Across alternative methods, both the bias and precision of the expected return measure can differ, affecting the properties of the abnormal return measures. Properties of different methods have been studied extensively, and are discussed later.

3.2 Statistical and economic hypotheses

Cross-sectional aggregation. An event study seeks to establish whether the cross-sectional distribution of returns at the time of an event is abnormal (i.e., systematically different from predicted). Such an exercise can be conducted in many ways. One could, for example, examine the entire distribution of abnormal returns. This is equivalent comparing the distributions of actual with the distribution of predicted returns and asking whether the distributions are the same. In the event study literature, the focus almost always is on the mean of the distribution of abnormal returns. Typically, the specific null hypothesis to be tested is whether the mean abnormal return (sometimes referred to as the average residual, AR) at time t is equal to zero. Other parameters of the cross-sectional distribution (e.g., median, variance) and determinants of the cross-sectional variation in abnormal returns are sometimes studied as well. The focus on mean effects, i.e., the first moment of the return distribution, makes sense if one

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3 For descriptions of each of these models, see Brown and Warner (1985) or Campbell, Lo, and MacKinlay (1997).
wants to understand whether the event is, on average, associated with a change in security holder
wealth, and if one is testing economic models and alternative hypotheses that predict the sign of
the average effect. For a sample of \( N \) securities, the cross-sectional mean abnormal return for
any period \( t \) is:

\[
AR_t = \frac{1}{N} \sum_{i=1}^{N} e_{it} .
\]  

\[ (3) \]

**Time-series aggregation.** It is also of interest to examine whether mean abnormal
returns for periods around the event are equal to zero. First, if the event is partially anticipated,
some of the abnormal return behavior related to the event should show up in the pre-event
period. Second, in testing market efficiency, the speed of adjustment to the information revealed
at the time of the event is an empirical question. Thus, examination of post-event returns
provides information on market efficiency.

In estimating the performance measure over any multi-period interval (e.g., time 0 through +6),
there are a number of methods for time-series aggregation over the period of
interest. The cumulative average residual method (CAR) uses as the abnormal performance
measure the sum of each month’s average abnormal performance. Later, we also consider the
buy-and-hold method, which first compounds each security’s abnormal returns and then uses the
mean compounded abnormal return as the performance measure. The CAR starting at time \( t_1 \)
through time \( t_2 \) (i.e., horizon length \( L = t_2 - t_1 + 1 \)) is defined as:

\[
CAR(t_1, t_2) = \sum_{t=t_1}^{t_2} AR_t .
\]  

\[ (4) \]

Both CAR and buy-and-hold methods test the null hypothesis that mean abnormal
performance is equal to zero. Under each method, the abnormal return measured is the same as
the returns to a trading rule which buys sample securities at the beginning of the first period, and holds through the end of the last period. CARs and buy-and-hold abnormal returns correspond to security holder wealth changes around an event. Further, when applied to post-event periods, tests using these measures provide information about market efficiency, since systematically nonzero abnormal returns following an event are inconsistent with efficiency and imply a profitable trading rule (ignoring trading costs).

3.3 Sampling distributions of test statistics

For a given performance measure, such as the CAR, a test statistic is typically computed and compared to its assumed distribution under the null hypothesis that mean abnormal performance equals zero. The null hypothesis is rejected if the test statistic exceeds a critical value, typically corresponding to the 5% or 1% tail region (i.e., the test level or size of the test is 0.05 or 0.01). The test statistic is a random variable because abnormal returns are measured with error. Two factors contribute to this error. First, predictions about securities’ unconditional expected returns are imprecise. Second, individual firms’ realized returns at the time of an event are affected for reasons unrelated to the event, and this component of the abnormal return does not average to literally zero in the cross-section.

For the CAR shown in equation (4), a standard test statistic is the CAR divided by an estimate of its standard deviation. Many alternative ways to estimate this standard deviation have been examined in the literature (see, for example, Campbell, Lo, and MacKinlay, 1997). The test statistic is given by:

4 Standard tests are “classical” rather than “Bayesian.” A Bayesian treatment of event studies is beyond the scope of this chapter.

5 An alternative would be a test statistic that aggregates standardized abnormal returns, which means each observation is weighted in inverse proportion of the standard deviation of the estimated abnormal return. The standard deviation of abnormal returns is estimated using time-series return data on each firm. While a test using standardized abnormal returns is in principle superior under certain conditions, empirically in short-horizon event studies it typically makes little difference (see Brown and Warner, 1980, and 1985).
\[
\frac{\text{CAR}(t_1, t_2)}{\left[\sigma^2(t_1, t_2)\right]^{1/2}}
\]

(5)

where

\[
\sigma^2(t_1, t_2) = L \sigma^2(AR_t)
\]

(6)

and \(\sigma^2(AR_t)\) is the variance of the one-period mean abnormal return. Equation (6) simply says that the CAR has a higher variance the longer is \(L\), and assumes time-series independence of the one-period mean abnormal return. The test statistic is typically assumed unit normal in the absence of abnormal performance. This is only an approximation, however, since estimates of the standard deviation are used.

The test statistic in eq. (5) is well-specified provided the variance of one-period mean abnormal return is estimated correctly. Event-time clustering renders the independence assumption for the abnormal returns in the cross-section incorrect (see Collins and Dent, 1984, Bernard, 1987, and Petersen, 2005, and more detailed discussion in section 4 below). This would bias the estimated standard deviation estimate downward and the test statistic given in eq. (5) upward. To address the bias, the significance of the event-period average abnormal return can be and often is gauged using the variability of the time series of event portfolio returns in the period preceding or after the event date. For example, the researcher can construct a portfolio of event firms and obtains a time series of daily abnormal returns on the portfolio for a number of days (e.g., 180 days) around the event date. The standard deviation of the portfolio returns can be used to assess the significance of the event-window average abnormal return. The cross-sectional dependence is accounted for because the variability of the portfolio returns through
time incorporates whatever cross-dependence that exists among the returns on individual event securities.

The portfolio return approach has a drawback, however. To the extent the event period is associated with increased uncertainty, i.e., greater return variability, the use of historical or post-event time-series variability might understate the true variability of the event-period abnormal performance. An increase in event-period return variability is economically intuitive. The event might have been triggered by uncertainty-increasing factors and/or the event itself causes uncertainty in the economic environment for the firm. In either case, the event-period return variability is likely to exceed that during other time periods for the event firms. Therefore, the statistical significance of the event-window abnormal performance would be overstated if it is evaluated on the basis of historical variability of the event-firm portfolio returns (see Brown and Warner, 1980, and 1985, and Collins and Dent, 1984). One means of estimating the likely increase in the variability of event-period returns is to estimate the cross-sectional variability of returns during the event and non-event periods. The ratio of the variances during the event period and non-event periods might serve as an estimate of the degree of increase in the variability of returns during the event period, which can be used to adjust for the bias in the test statistic calculated ignoring the increased event-period uncertainty.6

3.4 Criteria for “reliable” event study tests

Using the test statistics, errors of inference are of two types. A Type I error occurs when the null hypothesis is falsely rejected. A Type II error occurs when the null is falsely accepted. Accordingly, two key properties of event study tests have been investigated. The first is whether the test statistic is correctly specified. A correctly-specified test statistic yields a Type I error

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6 Use of non-parametric tests of significance, as suggested in Corrado (1989), might also be effective in performing well-specified tests in the presence of increased event-period uncertainty.
probability equal to the assumed size of the test. The second concern is power, i.e., a test’s ability to detect abnormal performance when it is present. Power can be measured as one minus the probability of a Type II error. Alternatively, it can be measured as the probability that the null hypothesis will be rejected given a level of Type I error and level of abnormal performance. When comparing tests that are well-specified, those with higher power are preferred.

3.5 Determining specification and power

The joint-test problem. While the specification and power of a test can be statistically determined, economic interpretation is not straightforward because all tests are joint tests. That is, event study tests are well-specified only to the extent that the assumptions underlying their estimation are correct. This poses a significant challenge because event study tests are joint tests of whether abnormal returns are zero and of whether the assumed model of expected returns (i.e. the CAPM, market model, etc.) is correct. Moreover, an additional set of assumptions concerning the statistical properties of the abnormal return measures must also be correct. For example, a standard t-test for mean abnormal performance assumes, among other things, that the mean abnormal performance for the cross-section of securities is normally distributed. Depending on the specific t-test, there may be additional assumptions that the abnormal return data are independent in time-series or cross-section. The validity of these assumptions is often an empirical question. This is particularly true for small samples, where one cannot rely on asymptotic results or the central limit theorem.

Brown-Warner simulation. To directly address the issue of event study properties, the standard tool in event study methodology research is simulation procedures that use actual security return data. The motivation and specific research design is initially laid out in Brown and Warner (1980, 1985), and has been followed in almost all subsequent methodology research.
Much of what is known about general properties of event study tests comes from such large-scale simulations. The basic idea behind the event study simulations is simple and intuitive. Different event study methods are simulated by repeated application of each method to samples that have been constructed through a random (or stratified random) selection of securities and random selection of an event date to each. If performance is measured correctly, these samples should show no abnormal performance, on average. This makes it possible to study test statistic specification, that is, the probability of rejecting the null hypothesis when it is known to be true. Further, various levels of abnormal performance can be artificially introduced into the samples. This permits direct study of the power of event study tests, that is, the ability to detect a given level of abnormal performance.

**Analytical methods.** Simulation methods seem both natural and necessary to determine whether event study test statistics are well-specified. Once it has been established using simulation methods that a particular test statistic is well-specified, analytical procedures have also been used to complement simulation procedures. Although deriving a power function analytically for different levels of abnormal performance requires additional distributional assumptions, the evidence in Brown and Warner (1985, p. 13) is that analytical and simulation methods yield similar power functions for a well-specified test statistic. As illustrated below, these analytical procedures provide a quick and simple way to study power.

### 3.6 A quick summary of our knowledge

**Qualitative properties.** Table 2 highlights, in qualitative terms, what is known about the properties of event study tests. The table shows the characteristics of event study methods along three dimensions: specification, power against specific types of alternative hypotheses, and the

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7 This characterization of simulation is from Brown and Warner (1985, p. 4).
sensitivity of specification to assumptions about the return generating process. The table also shows how these properties can differ sharply for short and long horizon studies. Much of the remainder of the chapter deals with the full details of this table.

From Table 2, horizon length has a big impact on event study test properties. First, short-horizon event study methods are generally well-specified, but long-horizon methods are sometimes very poorly specified. While much is understood about how to reduce misspecification in long horizon studies (see section 4), no procedure in whose specification researchers can have complete confidence has yet been developed. Second, short-horizon methods are quite powerful if (but only if) the abnormal performance is concentrated in the event window. For example, a precise event date is known for earnings announcements, but insider trading events might be known to have occurred only sometime during a one-month window. In contrast to the short-horizon tests, long-horizon event studies (even when they are well-specified) generally have low power to detect abnormal performance, both when it is concentrated in the event window and when it is not. That power to detect a given level of abnormal performance is decreasing in horizon length is not surprising, but the empirical magnitudes are dramatic (see below). Third, with short-horizon methods the test statistic specification is not highly sensitive to the benchmark model of normal returns or assumptions about the cross-sectional or time-series dependence of abnormal returns. This contrasts with long-horizon methods, where specification is quite sensitive to assumptions about the return generating process.

Along several lines, however, short- and long-horizon tests show similarities, and these results are easy to show using either simulation or analytical procedures. First, a common problem shared by both short- and long-horizon studies is that when the variance of a security’s
abnormal returns conditional on the event increases, test statistics can easily be misspecified, and reject the null hypothesis too often. This problem was first brought to light and has been studied mainly in the context of short-horizon studies (Brown and Warner, 1985, and Corrado, 1989). A variance increase is indistinguishable from abnormal returns differing across sample securities at the time of an event, and would be expected for an event. Thus, this issue is likely to be empirically relevant both in a short- and long-horizon context as well. Second, power is higher with increasing sample size, regardless of horizon length. Third, power depends on the characteristics of firms in the event study sample. In particular, firms experiencing a particular event can have nonrandom size and industry characteristics. This is relevant because individual security variances (and abnormal return variances) exhibit an inverse relation to firm size and can vary systematically by industry. Power is inversely related to sample security variance: the noisier the returns, the harder to extract a given signal. As shown below, differences in power by sample type can be dramatic.

**Quantitative results.** To provide additional texture on Table 2, below we show specific quantitative estimates of power. We do so using the test statistic shown previously in equations (5) and (6), using two-tailed tests at the 0.05 significance level. Since this test statistic is well-specified, at least at short horizons, the power functions are generated using analytic (rather than simulation) procedures. The estimates are for illustrative purposes only, however, and only represent “back of the envelope” estimates. The figures and the test statistic on which they are based assume independence of the returns (both through time and in the cross-section), and that all securities within a sample have the same standard deviation. The power functions also

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8 This format for displaying power functions is similar to Campbell, Lo, and MacKinlay (1997, pp. 168-172). Our test statistic and procedures are the same as for their test statistic J1, but as discussed below we use updated variance inputs.
assume that return and abnormal return variances are the same (i.e., the model of abnormal returns is the “mean-adjusted returns” model of Brown and Warner, 1980).

**Volatility.** In calculating the test statistic in an event study, a key input required here is the individual security return (or abnormal return) variance (or standard deviation). To determine a reasonable range of standard deviations, we estimate daily standard deviations for all CRSP listed firms from 1990 to 2002. Specifically, for each year, we: i) calculate each stock’s standard deviation, and ii) assign firms to deciles ranked by standard deviation. From each decile, the averages of each year’s mean and median values are reported in Table 3. The mean daily standard deviation for all firms is 0.053. This is somewhat higher than the value of 0.026 reported by Brown and Warner (1985, p. 9) for NYSE/AMEX firms and the value of 0.035 reported by Campbell and Wasley (1993, p. 79) for NASDAQ firms. The differences reflect that individual stocks have become more volatile over time (Campbell, Lettau, Malkiel, Xu, 2001)). This is highly relevant because it suggests that the power to detect abnormal performance for events over 1990-2002 is lower than for earlier periods. From Table 3, there is wide variation across the deciles. Firms in decile 1 have a mean daily standard deviation of 0.014, compared to 0.118 for decile 10. The figure of 0.118 for decile 10 seems very high, although this is likely to represent both very small firms and those with low stock prices. Further, there is a strong negative empirical relation between volatility and size. Our qualitative results apply if ranking is by firm size, so table 3 is not simply picking up measurement error in volatility.

**Results.** Figure 1 shows how, for a sample comprised of securities of average risk and 10% abnormal performance, the power to detect abnormal performance falls with horizon length. This level of abnormal performance seems economically highly significant. If the abnormal performance is concentrated entirely in one day (and the day in known with certainty), a sample
of only six stocks detects this level of abnormal performance 100% of the time. In contrast, if the same abnormal performance occurs over six months, a sample size of 200 is required to detect the abnormal performance even 65% of the time. These various rejection frequencies are lower than those using pre-1990 volatilities (not reported), although this is not surprising.

Figure 2a through 2c show related results using a one-day horizon for samples whose individual security standard deviations correspond to the average standard deviation for: the lowest decile (Figure 2a); all firms (Figure 2b); and the highest decile (Figure 2c). For decile 1 firms, with 1% abnormal performance a 90% rejection rate requires only 21 stocks. For firms in decile 10, even with 5% abnormal performance a 90% rejection rate requires 60 stocks. These comparisons may distort the differences in actual power if high variance firms are less closely followed and events are bigger surprises. When the effect of events differs cross-sectionally, analysis of test properties (i.e., power and specification) is more complicated.

Collectively, our results illustrate that power against alternative hypotheses can be sensitive to calendar time period and sample firm characteristics, and highlight the importance already recognized in the profession of studying test statistic properties for samples stratified by firm characteristics. A complete analysis of these issues would focus on abnormal return (rather than return) volatility, and study how specification (and abnormal return distributional properties such as skewness) varies across time and firm characteristics.

3.7 Cross-Sectional Tests

This section’s focus thus far has been event study tests for mean stock price effects. These tests represent the best understood class of event study tests. To provide a more complete the picture of event-related tests, we briefly call attention to cross-sectional tests. These tests
examine how the stock price effects of an event are related to firm characteristics. For a cross-
section of firms, abnormal returns are compared to (e.g., regressed against) firm characteristics. 
This provides evidence to discriminate among various economic hypotheses.

Cross-sectional tests are a standard part of almost every event study. They are relevant even when the mean stock price effect of an event is zero. In addition, they are applicable regardless of horizon length. They are simple to do, but as discussed below, “one must be careful in interpreting the results” (Campbell, Lo, and Mackinlay, 1997, p.174).

One reason that abnormal returns vary cross-sectionally is that the economic effect of the event differs by firm. For such a situation, Sefcik and Thompson (1986) examine the statistical properties of cross-sectional regressions. They are concerned with the effects of cross-sectionally correlated abnormal returns and heteroscedasticity in the abnormal returns. They argue that accounting for each appears to be potentially important for inferences, and they suggest procedures to deal with these issues.

Abnormal returns also vary cross-sectionally because the degree to which the event is anticipated differs by firm. For example, for firms which are more closely followed (e.g., more analysts), events should more predictable, all else equal. Further, events are endogenous, reflecting a firm’s self selection to choose the event, which in turn reflects insiders’ information. Recognizing these factors, and recognizing that it is the unexpected information provided by an event that determines the stock price effect, has numerous consequences. For example, standard estimates of cross-sectional coefficients can be biased (Eckbo, Maksimovic, and Williams (1990)). Appropriate procedures for treating self-selection and partial anticipation issues is the subject of an entire chapter by Li and Prabhala in this volume (see Ch 2).
Quite apart from the issues discussed in the context of Li and Prabha, there are several additional dimensions where our understanding of cross-sectional tests is incomplete, and where additional work is potentially fruitful. One area concerns the power of cross-sectional procedures. While specification of cross-sectional regression methods (i.e., biases in regression coefficients) has received much attention, the power of alternative procedures to detect underlying cross-sectional effects has received less study.

A related point is that a simple type of cross-sectional procedure is to form portfolios based on firm characteristics, and compare portfolio abnormal returns. Such procedures are common, but methodological comparisons to cross-sectional regressions would prove useful. Portfolio procedures seem less amenable to multivariate comparisons than do regression procedures, but the relative empirical merits of each in an event-study context have not been investigated.

We also note that some studies focus not on the stock price effect of an event, but on predicting a corporate event (e.g., management turnover, or a security issue of a particular type), sometimes using past stock prices as one explanatory variable. These tests use cross-sectional methods in the sense that the cross-section includes both event and non-event firms. Typically, discrete choice models (e.g., probit or logit model) relate whether or not the event occurred to firm-specific characteristics. This seems intuitive, since we would like to know what factors led the firm to have the event. These methods complement standard event study methods. Methodological work on prediction models could enhance our understanding of how to best to use information about events to test economic hypotheses about firm behavior.

Finally, additional important issues to consider in an event study are: (i) whether the event was partially anticipated by market participants (e.g., a governance-related regulation
might be anticipated following corporate scandals or CEO turnover is likely in the case of a firm experiencing steep stock-price decline and poor accounting performance), and (ii) whether the partial anticipation is expected to vary cross-sectionally in a predictable fashion (e.g., market participants might anticipate that managers of firms experiencing high price run-ups are likely to make value-destroying stock acquisitions, but the negative announcement effect of an actual merger announcement might have been largely anticipated for the firms who have experienced relatively high prior price run up). These issues arising from the nature of information arrival, partial anticipation of events, and cross-sectional variation in the degree of anticipation are also beyond the scope of this chapter. Interested readers will find treatments in Malatesta and Thompson (1985), Eckbo, Maksimovic, and Williams (1990), and, especially, Thompson (1995) of considerable interest.

4. Long-Horizon Event Studies

All event studies, regardless of horizon length, must deal with several basic issues. These include risk adjustment and expected/abnormal return modeling (Section 4.2), the aggregation of security-specific abnormal returns (Section 4.3), and the calibration of the statistical significance of abnormal returns (Section 4.4). These issues become critically important with long horizons. The remainder of this chapter focuses on efforts in the long-horizon literature to deal with the issues

4.1 Background

Long-horizon event studies have a long history, including the original stock split event study by Fama, Fisher, Jensen, and Roll (1969). As evidence inconsistent with the efficient markets hypothesis started to accumulate in the late seventies and early eighties, interest in long-
horizon studies intensified. Evidence on the post-earnings announcement effect (see Ball and Brown, 1968, and Jones and Litzenberger, 1970), size effect (Banz, 1981), and earnings yield effect (Basu, 1977 and 1983) contributed to skepticism about the CAPM as well as market efficiency. This evidence prompted researchers to develop hypotheses about market inefficiency stemming from investors’ information processing biases (see DeBondt and Thaler, 1985 and 1987) and limits to arbitrage (see DeLong et al., 1990a and 1990b, and Shleifer and Vishny, 1997).

The “anomalies” literature and the attempts to model the anomalies as market inefficiencies has led to a burgeoning field known as behavioral finance. Research in this field formalizes (and tests) the security pricing implications of investors’ information processing biases.9 Because the behavioral biases might be persistent and arbitrage forces might take a long time to correct the mispricing, a vast body of literature hypothesizes and studies abnormal performance over long horizons of one-to-five years following a wide range of corporate events. The events might be one-time (unpredictable) phenomena like an initial public offering or a seasoned equity offering, or they may be recurring events such as earnings announcements.

Many long-horizon studies document apparent abnormal returns spread over long horizons. The literature on long-horizon security price performance following corporate events is summarized extensively in many studies, including Fama (1998), Kothari and Warner (1997), Schwert (2001), and Kothari (2001). Whether the apparent abnormal returns are due to mispricing, or simply the result of measurement problems, is a contentious and unresolved issue among financial economists. The methodological research in the area is important because it

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demonstrates how easy it is to conclude there is abnormal performance when none exists. Before questions on mispricing can be answered, better methods than currently exist are required.


4.2 Risk adjustment and expected returns

In long-horizon tests, appropriate adjustment for risk is critical in calculating abnormal price performance. This is in sharp contrast to short-horizon tests in which risk adjustment is straightforward and typically unimportant. The error in calculating abnormal performance due to errors in adjusting for risk in a short-horizon test is likely to be small. Daily expected returns are about 0.05% (i.e., annualized about 12-13%). Therefore, even if the event firm portfolio’s beta risk is misestimated by 50% (e.g., estimated beta risk of 1.0 when true beta risk is 1.5), the error in the estimated abnormal error is small relative to the abnormal return of 1% or more that is typically documented in short-window event studies. Not surprisingly, Brown and Warner (1985) conclude that simple risk-adjustment approaches to conducting short-window event studies are quite effective in detecting abnormal performance.

In multi-year long-horizon tests, risk-adjusted return measurement is the Achilles heel for at least two reasons. First, even a small error in risk adjustment can make an economically large difference when calculating abnormal returns over horizons of one year or longer, whereas such errors make little difference for short horizons. Thus the precision of the risk adjustment becomes far more important in long-horizon event studies. Second, it is unclear which expected
return model is correct, and therefore estimates of abnormal returns over long horizons are highly sensitive to model choice. We now discuss each of these problems in turn.

**Errors in risk adjustment.** Such errors can make an economically non-trivial difference in measured abnormal performance over one-year or longer periods. The problem of risk adjustment error is exacerbated in long-horizon event studies because the potential for such error is greater for longer horizons. In many event studies, (i) the event follows unusual prior performance (e.g., stock splits follow good performance), or (ii) the event sample consists of firms with extreme (economic) characteristics (e.g., low market capitalization stocks, low-priced stocks, or extreme book-to-market stocks), or (iii) the event is defined on the basis of unusual prior performance (e.g., contrarian investment strategies in DeBondt and Thaler, 1985, and Lakonishok, Shleifer, and Vishny, 1994). Under these circumstances, accurate risk estimation is difficult, with historical estimates being notoriously biased because prior economic performance negatively impacts the risk of a security. Therefore, in long-horizon event studies, it is crucial that abnormal-performance measurement be on the basis of post-event, not historical risk estimates (see Ball and Kothari, 1989, Chan, 1988, and Ball, Kothari, and Shanken, 1995, and Chopra, Lakonishok, and Ritter, 1992). However, how the post-event risk should be estimated is itself a subject of considerable debate, which we summarize below in an attempt to offer guidance to researchers.

**Model for expected returns.** The question of which model of expected returns is appropriate remains an unresolved issue. As noted earlier, event studies are joint tests of market efficiency and a model of expected returns (e.g., Fama, 1970). On a somewhat depressing note, Fama (1998, p. 291) concludes that “all models for expected returns are incomplete descriptions of the systematic patterns in average returns,” which can lead to spurious indications of abnormal
performance in an event study. With the CAPM as a model of expected returns being thoroughly discredited as a result of the voluminous anomalies evidence, a quest for a better-and-improved model began. The search culminated in the Fama and French (1993) three-factor model, further modified by Carhart (1997) to incorporate the momentum factor. However, absent a sound economic rationale motivating the inclusion of the size, book-to-market, and momentum factors, whether these factors represent equilibrium compensation for risk or they are an indication of market inefficiency has not been satisfactorily resolved in the literature (see, e.g., Brav and Gompers, 1997). Fortunately, from the standpoint of event study analysis, this flaw is not fatal. Regardless of whether the size, book-to-market, and momentum factors proxy for risk or indicate inefficiency, it is essential to use them when measuring abnormal performance. The purpose of an event study is to isolate the incremental impact of an event on security price performance. Since the price performance associated with the size, book-to-market, and momentum characteristics is applicable to all stocks sharing those characteristics, not just the sample of firms experiencing the event (e.g., a stock split), the performance associated with the event itself must be distinguished from that associated with other known determinants of performance, such as the aforementioned four factors.

4.3 Approaches to abnormal performance measurement

While post-event risk-adjusted performance measurement is crucial in long-horizon tests, actual measurement is not straightforward. Two main methods for assessing and calibrating post-event risk-adjusted performance are used: characteristic-based matching approach and the Jensen’s alpha approach, which is also known as the calendar-time portfolio approach (see Fama,

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10 More recently, considerable accumulated evidence suggests the importance of a liquidity factor in determining expected returns (see Brennan and Subrahmanyam, 1996, Pastor and Stambaugh, 2003, and Sadka, 2006).

11 See Kothari, Leone, and Wasley (2005) for an extended discussion.
1998, Eckbo, Masulis, and Norli, 2000, or Mitchell and Stafford, 2000). Analysis and comparison of the methods is detailed below. Despite an extensive literature, there is still no clear winner in a horse race. Both have low power against economically interesting null hypotheses, and neither is immune to misspecification.

4.3.1 BHAR approach

In recent years, following the works of Ikenberry, Lakonishok, and Vermaelen (1995), Barber and Lyon (1997), Lyon et al. (1999), the characteristic-based matching approach (or also known as the buy-and-hold abnormal returns, BHAR) has been widely used. Mitchell and Stafford (2000, p. 296) describe BHAR returns as “the average multiyear return from a strategy of investing in all firms that complete an event and selling at the end of a prespecified holding period versus a comparable strategy using otherwise similar nonevent firms.” An appealing feature of using BHAR is that buy-and-hold returns better resemble investors’ actual investment experience than periodic (monthly) rebalancing entailed in other approaches to measuring risk-adjusted performance.12 The joint-test problem remains in that any inference on the basis of BHAR hinges on the validity of the assumption that event firms differ from the “otherwise similar nonevent firms” only in that they experience the event. The researcher implicitly assumes an expected return model in which the matched characteristics (e.g., size and book-to-market) perfectly proxy for the expected return on a security. Since corporate events themselves are unlikely to be random occurrences, i.e., they are unlikely to be exogenous with respect to past performance and expected returns, there is a danger that the event and nonevent samples differ systematically in their expected returns notwithstanding the matching on certain firm characteristics.

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12 Apart from similarity with the actual investment experience, the BHAR approach also avoids biases arising from security microstructure issues when portfolio performance is measured with frequent rebalancing (see Blume and Stambaugh, 1983, Roll, 1983, and Ball, Kothari, and Shanken, 1995). The latter biases are also reduced if value-weight portfolio performance is examined.
characteristics. This makes matching on (unobservable) expected returns more difficult, especially in the case of event firms experiencing extreme prior performance.

Once a matching firm or portfolio is identified, BHAR calculation is straightforward. A T-month BHAR for event firm $i$ is defined as:

$$\text{BHAR}_i(t, T) = \prod_{t=1}^{T} (1 + R_{i,t}) - \prod_{t=1}^{T} (1 + R_{B,t})$$

where $R_B$ is the return on either a non-event firm that is matched to the event firm $i$, or it is the return on a matched (benchmark) portfolio.\(^{13}\) If the researcher believes that the Carhart (1997) four-factor model is an adequate description of expected returns, then firm-specific matching might entail identifying a non-event firm that is closest to an event firm on the basis of firm size (i.e., market capitalization of equity), book-to-market ratio, and past one-year return. Alternatively, characteristic portfolio matching would identify the portfolio of all non-event stocks that share the same quintile ranking on size, book-to-market, and momentum as the event firm (see Daniel, Grinblatt, Titman, and Wermers, 1997, or Lyon, Barber, and Tsai, 1997, for details of benchmark portfolio construction). The return on the matched portfolio is the benchmark portfolio return, $R_B$. For the sample of event firms, the mean BHAR is calculated as the (equal- or value-weighted) average of the individual firm BHARs.

### 4.3.2 Jensen-alpha approach

The Jensen-alpha approach (or the calendar-time portfolio approach) to estimating risk-adjusted abnormal performance is an alternative to the BHAR calculation using a matched-firm approach to risk adjustment. Jaffe (1974) and Mandelker (1974) introduced a calendar time methodology to the financial-economics literature, and it has since been advocated by many,\(^{13}\)

\(^{13}\) See Mitchell and Stafford (2000) for details.
including Fama (1998) and Mitchell and Stafford (2000). The distinguishing feature of the most recent variants of the approach is to calculate calendar-time portfolio returns for firms experiencing an event, and calibrate whether they are abnormal in a multifactor (e.g., CAPM or Fama-French three factor) regression. The estimated intercept from the regression of portfolio returns against factor returns is the post-event abnormal performance of the sample of event firms.

To implement the Jensen-alpha approach, assume a sample of firms experiences a corporate event (e.g., an IPO or an SEO). The event might be spread over several years or even many decades (the sample period). Also assume that the researcher seeks to estimate price performance over two years (T = 24 months) following the event for each sample firm. In each calendar month over the entire sample period, a portfolio is constructed comprising all firms experiencing the event within the previous T months. Because the number of event firms is not uniformly distributed over the sample period, the number of firms included in a portfolio is not constant through time. As a result, some new firms are added each month and some firms exit each month. Accordingly, the portfolios are rebalanced each month and an equal or value-weighted portfolio excess return is calculated. The resulting time series of monthly excess returns is regressed on the CAPM market factor, or the three Fama-French (1993) factors, or the four Carhart (1997) factors as follows:

\[ R_{pt} - R_n = a_p + b_p (R_{mt} - R_n) + s_p \text{SMB}_t + h_p \text{HML}_t + m_p \text{UMD}_t + e_{pt} \]  

(8)

where

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14 For a variation of the Jensen-alpha approach, see Ibbotson (1975) returns across time and securities (RATS) methodology, which is used in Ball and Kothari (1989) and others.

15 The description here is based on Mitchell and Stafford (2000).
Rpt is the equal or value-weighted return for calendar month t for the portfolio of event firms that experienced the event within the previous T months,

Rf is the risk-free rate,

Rmt is the return on the CRSP value-weight market portfolio,

SMBpt is the difference between the return on the portfolio of “small” stocks and “big” stocks;

HMLpt is the difference between the return on the portfolio of “high” and “low” book-to-market stocks;

UMDpt is the difference between the return on the portfolio of past one-year “winners” and “losers,”

ap is the average monthly abnormal return (Jen sen alpha) on the portfolio of event firms over the T-month post-event period,

bp, sp, hp, and mp are sensitivities (betas) of the event portfolio to the four factors.

Inferences about the abnormal performance are on the basis of the estimated ap and its statistical significance. Since ap is the average monthly abnormal performance over the T-month post-event period, it can be used to calculate annualized post-event abnormal performance.

Recent work on the implications of using the Jensen-alpha approach is mixed. For example, Mitchell and Stafford (2000) and Brav and Gompers (1997) favor the Jensen-alpha approach. However, Loughran and Ritter (2000) argue against using the Jensen-alpha approach because it might be biased toward finding results consistent with market efficiency. Their rationale is that corporate executives time the events to exploit mispricing, but the Jensen-alpha approach, by forming calendar-time portfolios, under-weights managers’ timing decisions and over-weights other observations. In the words of Loughran and Ritter (2000, p. 362): “If there are time-varying misvaluations that firms capitalize on by taking some action (a supply response), there will be more events involving larger misvaluations in some periods than in others……In general, tests that weight firms equally should have more power than tests that
weight each time period equally.” Since the Jensen-alpha (i.e., calendar-time) approach weights each period equally, it has lower power to detect abnormal performance if managers time corporate events to coincide with misvaluations. As a means of addressing the problem, Fama (1998) advocates weighting calendar months by their statistical precision, which varies with sample size. Countering the criticism of Loughran and Ritter (2000), Eckbo et al. (2000) point out another problem with the buy-and-hold abnormal return methods. The latter is not a feasible portfolio strategy because the total number of securities is not known in advance.\textsuperscript{16}

4.4 Significance tests for BHAR and Jensen-alpha measures

The choice between the matched-firm BHAR approach to abnormal return measurement and the calendar time Jensen-alpha approach (also known as the calendar-time portfolio approach) hinges on the researcher’s ability to accurately gauge the statistical significance of the estimated abnormal performance using the two approaches. Unbiased standard errors for the distribution of the event-portfolio abnormal returns are not easy to calculate, which leads to test misspecification. Assessing the statistical significance of the event portfolio’s BHAR has been particularly difficult because (i) long-horizon returns depart from the normality assumption that underlies many statistical tests; (ii) long-horizon returns exhibit considerable cross-correlation because the return horizons of many event firms overlap and also because many event firms are drawn from a few industries; and (iii) volatility of the event firm returns exceeds that of matched firms because of event-induced volatility. We summarize below the econometric inferential

\textsuperscript{16} The BHAR approach is also criticized for “pseudo-timing” because BHAR mechanically produces underperformance following a clustering of issues experiencing a common event, e.g., an IPO, in an up or down market (see Schultz, 2003, and Eckbo and Norli, 2005). The criticism assumes that those seeking to exploit the event-related market inefficiency do not have market-timing ability. The question of pseudo-timing and return predictability is a topic of intense current interest and appears currently unresolved (see Baker, Talliaferro, and Wurgler, 2004 and 2006, Goyal and Welch, 2003 and 2005, Boudoukh, Richardson, and Whitelaw, 2006, and Cochrane, 2006).
issues encountered in performing long-horizon tests and some of the remedies put forward in recent studies.

4.4.1 Skewness

Long-horizon buy-and-hold returns, even after adjusting for the performance of a matched firm (or portfolio), tend to be right skewed. The right skewness of buy-and-hold returns is not surprising because the lower bound is -100% and returns are unbounded on the upside. Skewness in abnormal returns imparts a skewness bias to long-horizon abnormal performance test statistics (see Barber and Lyon, 1997). Brav (2000, p. 1981) concludes that “with a skewed-right distribution of abnormal returns, the Student t-distribution is asymmetric with a mean smaller than the zero null.” While the right-skewness of individual firms’ long-horizon returns is undoubtedly true, the extent of skewness bias in the test statistic for the hypothesis that mean abnormal performance for the portfolio of event firms is zero is expected to decline with sample size.17 Fortunately, the sample size in long-horizon event studies is often several hundred observations (e.g., Teoh, Welch, and Wong, 1998, and Byun and Rozeff, 2003). Therefore, if the BHAR observations for the sample firms are truly independent, as assumed in using a t-test, the Central Limit Theorem’s implication that “the sum of a large number of independent random variables has a distribution that is approximately normal” should apply (Ross, 1976, p. 252). The right-skewness of the distribution of long-horizon abnormal returns on event portfolios, as documented in, for example, Brav (2000) and Mitchell and Stafford (2000), appears to be due largely to the lack of independence arising from overlapping long-horizon return observations in event portfolios. That is, skewness in portfolio returns is in part a by-product of cross-correlated

17 Simulation evidence in Barber and Lyon (1997) on skewness bias is based on samples consisting of 50 firms and early concern over skewness bias as examined in Neyman and Pearson (1928) and Pearson (1929a and 1929b) also refers to skewness bias in small samples.
data rather than a direct consequence of skewed firm-level buy-and-hold abnormal (or raw) returns.

4.4.2 Cross-correlation

The issue. Specification bias arising due to cross-correlation in returns is a serious problem in long-horizon tests of price performance. Brav (2000, p. 1979) attributes the misspecification to the fact that researchers conducting long-horizon tests typically “maintain the standard assumptions that abnormal returns are independent and normally distributed although these assumptions fail to hold even approximately at long horizons.”18 The notion that economy-wide and industry-specific factors would generate contemporaneous co-movements in security returns is the cornerstone of portfolio theory and is economically intuitive and empirically compelling. Interestingly, the cross-dependence, although muted, is also observed in risk-adjusted returns.19 The degree of cross-dependence decreases in the effectiveness of the risk-adjustment approach and increases in the homogeneity of the sample firms examined (e.g., sample firms clustered in one industry). Cross-correlation in abnormal returns is largely irrelevant in short-window event studies when the event is not clustered in calendar time. However, in long-horizon event studies, even if the event is not clustered in calendar time, cross-correlation in abnormal returns cannot be ignored (see Brav, 2000, Mitchell and Stafford, 2000, and Jegadeesh and Karceski, 2004). Long-horizon abnormal returns tend to be cross-correlated because: (i) abnormal returns for subsets of the sample firms are likely to share a common calendar period due to the long measurement period; (ii) corporate events like mergers and share

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repurchases exhibit waves (for rational economic reasons as well as opportunistic actions on the part of the shareholders and/or management); and (iii) some industries might be over-represented in the event sample (e.g., merger activity among technology stocks).

If the test statistic in an event study is calculated ignoring cross-dependence in data, even a fairly small amount of cross-correlation in data will lead to serious misspecification of the test. In particular, the test will reject the null of no effect far more often than the size of the test (see Collins and Dent, 1984, Bernard, 1987, and Mitchell and Stafford, 2000). The overrejection is caused by the downward biased estimate of the standard deviation of the cross-sectional distribution of buy-and-hold abnormal returns for the event sample of firms.

**Magnitude of bias.** To get an idea of approximate magnitude of the bias, we begin with the cross-sectional standard deviation of the event firms’ abnormal returns, AR, assuming equal variances and pairwise covariances across all sample firms’ abnormal returns:

\[
\sigma_{AR} = \left[ \left( \frac{1}{N} \right) \sigma^2 + \left( \frac{N - 1}{N} \right) (\rho_{ij} \sigma^2) \right]^{1/2} \quad (9)
\]

where \( N \) is the number of sample firms, \( \sigma^2 \) is the variance of abnormal returns, which is assumed to be the same for all firms; and \( \rho_{ij} \) is the correlation between firm i and j’s abnormal returns, which is also assumed to be the same across all firms. The second term in the square brackets in eq. (9) is due to the cross-dependence in the data, and it would be absent if the standard deviation is calculated assuming independence in the data. The bias in the standard deviation assuming independence is given by the ratio of the “true” standard deviation allowing for dependence to the standard deviation assuming independence:

\[
\sigma_{AR} \text{ (Dependence)} / \sigma_{AR} \text{ (Independence)} = \left[ 1 + (N - 1) \rho_{ij} \right]^{1/2} \quad (10)
\]

The ratio in eq. (10) is the factor by which the standard error in a test for the significance of abnormal performance is understated and therefore the factor by which the test statistic (e.g.,
t-statistic) itself is overstated. The ratio is increasing in the pairwise cross-correlation, $\rho_{ij}$. Empirical estimates of the average pairwise correlation between annual BHARs of event firms are about 0.02 to 0.03 (see Mitchell and Stafford, 2000). The average pairwise correlation in multi-year BHARs is likely to be greater than that for annual returns because Bernard (1987, table 1) reports that the average cross-correlations increase with return horizon. Assuming the average pairwise cross-sectional correlation to be only 0.02, for a sample of 100, the ratio is eq. (4) is 1.73, and it increases with both sample size and the degree of cross-correlation. Since the sample size in many long-horizon event studies is a few hundred securities, and the BHAR horizon is three-to-five years, even a modest degree of average cross-correlation in the data can inflate the test statistics by a factor of two or more. Therefore, accounting for cross-correlation in abnormal returns is crucial to drawing accurate statistical inferences in long-horizon event studies. Naturally, this has been a subject of intense interest among researchers.

**Potential solutions.** One simple solution to the potential bias due to cross-correlation is to use the Jensen-alpha approach. It is immune to the bias arising from cross-correlated (abnormal) returns because of the use of calendar-time portfolios. Whatever the correlation among security returns, the event portfolio’s time series of returns in calendar time accounts for that correlation. That is, the variability of portfolio returns is influenced by the cross-correlation in the data. The statistical significance of the Jensen alpha is based on the time-series variability of the portfolio return residuals. Since returns in an efficient market are serially uncorrelated (absent nontrading), on this basis the independence assumption in calculating the standard error and the t-statistic for the regression intercept (i.e., the Jensen alpha) seems quite appropriate. However, the evidence is that this method is misspecified in nonrandom samples (Lyon et al., 1999, Table 10). This is unfortunate, given that the method seems simple and direct. The
reasons for the misspecification are unclear (see Lyon et al.). Appropriate calibration under calendar time methods probably warrants further investigation.

In the BHAR approach, estimating standard errors that account for the cross-correlation in long-horizon abnormal returns is not straightforward. As detailed below, there has been much discussion, and some interesting progress. Statistically precise estimates of pairwise cross-correlations are difficult to come by for the lack of availability of many time-series observations of long-horizon returns to accurately estimate the correlations (see Bernard, 1987). The difficulty is exacerbated by the fact that only a portion of the post-event-period might overlap with other firms. Researchers have developed bootstrap and pseudoportfolio-based statistical tests that might account for the cross-correlations and lead to accurate inferences.

**Cross-correlation and skewness.** Lyon et al. (1999) develop a bootstrapped skewness-adjusted t-statistic to address the cross-correlation and skewness biases. The first step in the calculation is the skewness-adjusted t-statistic (see Johnson, 1978). This statistic adjusts the usual t-statistic by two terms that are a function of the skewness of the distribution of abnormal returns (see eq. 5 in Lyon et al., 1999, p. 174). Notwithstanding the skewness adjustment, the adjusted t-statistic indicates overrejection of the null and thus warrants a further refinement. The second step, therefore, is to construct a bootstrapped distribution of the skewness-adjusted t-statistic (see Sutton, 1993, and Lyon et al., 1999). To bootstrap the distribution, a researcher must draw a large number (e.g., 1,000) of resamples from the original sample of abnormal returns and calculate the skewness-adjusted t-statistic using each resample. The resulting empirical distribution of the test statistics is used to ascertain whether the skewness-adjusted t-statistic for the original event sample falls in the $\alpha\%$ tails of the distribution to reject the null hypothesis of zero abnormal performance.
The pseudoportfolio-based statistical tests infer statistical significance of the event sample’s abnormal performance by calibrating against an empirical distribution of abnormal performance constructed using repeatedly-sampled pseudoportfolios.\textsuperscript{20} The empirical distribution of average abnormal returns on the pseudoportfolios is under the null hypothesis of zero abnormal performance. The empirical distribution is generated by repeatedly constructing matched firm samples with replacement. The matching is on the basis of characteristics thought to be correlated with the expected rate of return. Following the Fama and French (1993) three-factor model, matching on size and book-to-market as expected return determinants is quite common (e.g., Lyon et al., 1999, Byun and Rozeff, 2003, and Gompers and Lerner, 2003). For each matched-sample portfolio, an average buy-and-hold abnormal performance is calculated as the raw return minus the benchmark portfolio return. It’s quite common to use 1,000 to 5,000 resampled portfolios to construct the empirical distribution of the average abnormal returns on the matched-firm samples. This distribution yields empirical 5 and 95% cut-off probabilities against which the event-firm sample’s performance is calibrated to infer whether or not the event-firm portfolio buy-and-hold abnormal return is statistically significant.

Unfortunately, the two approaches described above, which are aimed at correcting the bias in standard errors due to cross-correlated data, are not quite successful in their intended objective. Lyon et al. find pervasive test misspecification in non-random samples. Because the sample of firms experiencing a corporate event is not selected randomly by the researcher, correcting for the bias in the standard errors stemming from the non-randomness of the event sample selection is not easy. In a strident criticism of the use of bootstrap- and pseudoportfolio-

based tests, Mitchell and Stafford (2000, p. 307) conclude that long-term event studies often incorrectly “claim that bootstrapping solves all dependence problems. However, that claim is not valid. Event samples are clearly different from random samples. Event firms have chosen to participate in a major corporate action, while nonevent firms have chosen to abstain from the action. An empirical distribution created by randomly selecting firms with similar size-BE/ME characteristics does not replicate the covariance structure underlying the original event sample. In fact, the typical bootstrapping approach does not even capture the cross-sectional correlation structure related to industry effects….” Jegadeesh and Karceski (2004, pp. 1-2) also note that the Lyon et al. (1999) approach is misspecified because it “assumes that the observations are cross-sectionally uncorrelated. This assumption holds in random samples of event firms, but is violated in nonrandom samples. In nonrandom samples where the returns for event firms are positively correlated, the variability of the test statistics is larger than in a random sample. Therefore, if the empiricist calibrates the distribution of the test statistics in random samples and uses the empirical cutoff points for nonrandom samples, the tests reject the null hypothesis of no abnormal performance too often.”

**Autocorrelation.** To overcome the weaknesses in prior tests, Jegadeesh and Karceski (2004) propose a correlation and heteroskedasticity-consistent test. The key innovation in their approach is to estimate the cross-correlations using a monthly time-series of portfolio long-horizon returns (see Jegadeesh and Karceski, 2004, section II.A for details). Because the series is monthly, but the monthly observations contain long-horizon returns, the time-series exhibits autocorrelation that is due to overlapping return data. The autocorrelation is, of course, due to cross-correlation in return data. The autocorrelation is expected to be positive for H-1 lags, where H is the number of months in the long horizon. The length of the time-series of monthly
observations depends on the sample period during which corporate events being examined take place. Because of autocorrelation in the time series of monthly observations, the usual t-statistic that is a ratio of the average abnormal return to the standard deviation of the time series of the monthly observations would be understated. To obtain an unbiased t-statistic, the covariances (i.e., the variance-covariance matrix) should be taken into account. Jegadeesh and Karceski (2004) use the Hansen and Hodrick (1980) estimator of the variance-covariance matrix assuming homoskedasticity. They also use a heteroskedasticity-consistent estimator that “generalizes White’s heteroskedasticity-consistent estimator and allows for serial covariances to be non-zero” (p. 8). In both random and non-random (industry) samples the Jegadeesh and Karceski (2004) tests perform quite well, and we believe these might be the most appropriate to reduce misspecification in tests of long-horizon event studies.

4.4.3 The bottom line

Despite positive developments in BHAR calibration methods, two general long-horizon problems remain. The first concerns power. Jegadeesh and Karceski report that their tests show no increase in power relative to that of the test employed in previous research, which already had low power. For example, even with seemingly huge cumulative abnormal performance (25% over 5 years) in a sample of 200 firms, the rejection rate of the null is typically under 50% (see their Table 6).

Second, specification issues remain. For example, as discussed earlier (Section 3.6), events are generally likely to be associated with variance increases, which are equivalent to abnormal returns varying across sample securities. Previous literature shows that variance increases induce misspecification, and can cause the null hypothesis to be rejected far too often.
Thus, whether a high level of measured abnormal performance is due to chance or mispricing (or a bad model) is still difficult to empirically determine, unless the test statistic is adjusted downward to reflect the variance shift. Solutions to the variance shift issue include such intuitive procedures as forming subsamples with common characteristics related to the level of abnormal performance (e.g., earnings increase vs. decrease subsamples). With smaller subsamples, however, specification issues unrelated to variance shifts become more relevant. Moreover, the importance of examining specification for nonrandom samples cannot be overemphasized.

Given the various power and specification issues, a challenge that remains for the profession is to continue to refine long-horizon methods. Whether calendar time, BHAR methods or some combination can best address long-horizon issues remains an open question.
References


Cochrane, J., 2006, The dog that did not bark: A defense of return predictability, working paper, University of Chicago and NBER.


Pearson, E., (1929a), The distribution of frequency constants in small samples from symmetrical distributions, Biometrika 21: 356-360.

Pearson, E., (1929b), The distribution of frequency constants in small samples from non-normal symmetrical and skew populations, Biometrika 21: 259-286.


Table 1
Event studies, by year and journal. For each journal, all papers that contain an event study are included. Survey and methodological papers are excluded.

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Totals  | 44  | 212  | 207  | 82  | 20  | 565  |
Table 2
General characterization of properties of event study test methods.

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<th>Criterion</th>
<th>Length of Event Window</th>
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<td>Short (&lt; 12 months)</td>
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<td><strong>Specification</strong></td>
<td>Good</td>
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<tr>
<td><strong>Power when abnormal performance is:</strong></td>
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<tr>
<td>Concentrated in event window</td>
<td>High</td>
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<tr>
<td>Not concentrated in event window</td>
<td>Low</td>
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<tr>
<td><strong>Sensitivity of test statistic specification to assumptions about the return generating process:</strong></td>
<td></td>
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<tr>
<td>Expected returns, unconditional on event</td>
<td>Low</td>
</tr>
<tr>
<td>Cross-sectional and time-series dependence of sample abnormal returns</td>
<td>Low/Moderate</td>
</tr>
<tr>
<td>Variance of abnormal returns, conditional on event</td>
<td>High</td>
</tr>
<tr>
<td><strong>Sensitivity of power to:</strong></td>
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<tr>
<td>Sample size</td>
<td>High</td>
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<tr>
<td>Firm characteristics (e.g., size, industry)</td>
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Table 3  
Standard deviation of daily returns on individual securities using all CRSP common-stock securities from 1990-2002. For each year, firms are ranked by their estimated daily standard deviation. Firms with missing observations are excluded. The numbers under mean and median columns represent the average of the annual mean and median values for the firms in each decile and for all firms. The number of firms in each decile ranges from 504 in 2002 to 673 in 1997.

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<td>All Firms</td>
<td><strong>0.053</strong></td>
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</table>
Figure 1: Power of event study test statistic when abnormal return is 10%.

Figure 2a: Power of event study for firms in the lowest volatility decile.
Figure 2b: Power of event study for firms with average volatility

Figure 2c: Power of event study for firms in the highest volatility decile.